National Association of Special Education Teachers (NASET)

THE PRACTICAL TEACHER

This Month's Topic:

Math Problem-Solving: Combining Cognitive & Metacognitive Strategies in a 7-Step Process

Solving an advanced math problem independently requires the coordination of a number of complex skills. The student must have the capacity to reliably implement the specific steps of a particular problem-solving process, or cognitive strategy. At least as important, though, is that the student must also possess the necessary metacognitive skills to analyze the problem, select an appropriate strategy to solve that problem from an array of possible alternatives, and monitor the problem-solving process to ensure that it is carried out correctly.

The following strategies combine both cognitive and metacognitive elements (Montague, 1992; Montague & Dietz, 2009). First, the student is taught a 7-step process for attacking a math word problem (cognitive strategy). Second, the instructor trains the student to use a three-part self-coaching routine for each of the seven problem-solving steps (metacognitive strategy).

In the cognitive part of this multi-strategy intervention, the student learns an explicit series of steps to analyze and solve a math problem. Those steps include:

- 1. Reading the problem. The student reads the problem carefully, noting and attempting to clear up any areas of uncertainly or confusion (e.g., unknown vocabulary terms).
- **2. Paraphrasing the problem.** The student restates the problem in his or her own words.
- 3. 'Drawing' the problem. The student creates a drawing of the problem, creating a visual representation of the word problem.
- **4.** Creating a plan to solve the problem. The student decides on the best way to solve the problem and develops a plan to do so.
- **5. Predicting/Estimating the answer.** The student estimates or predicts what the answer to the problem will be. The student may compute a quick approximation of the answer, using rounding or other shortcuts.

- **6.** Computing the answer. The student follows the plan developed earlier to compute the answer to the problem.
- 7. Checking the answer. The student methodically checks the calculations for each step of the problem. The student also compares the actual answer to the estimated answer calculated in a previous step to ensure that there is general agreement between the two values.

The metacognitive component of the intervention is a three-part routine that follows a sequence of 'Say', 'Ask, 'Check'. For each of the 7 problem-solving steps reviewed above:

- The student first self-instructs by stating, or 'saying', the purpose of the step ('Say').
- The student next self-questions by 'asking' what he or she intends to do to complete the step ('Ask').
- The student concludes the step by self-monitoring, or 'checking', the successful completion of the step ('Check').

While the Say-Ask-Check sequence is repeated across all 7 problem-solving steps, the actual content of the student self-coaching comments changes across the steps.

Table 1 shows how each of the steps in the word problem cognitive strategy is matched to the three-part Say-Ask-Check sequence:

Table 1: 'Say-Ask-Check' Metacognitive Prompts Tied to a Word-Problem Cognitive Strategy (Montague, 1992)					
Cognitive		Metacognitive 'Say-Ask-Check' Prompt	Sample Metacognitive 'Say-Ask-Check'		
Strategy Step		Targets	Prompts		
1.	Read the	'Say' (Self-Instruction) Target: The student	Say: "I will read the problem. I will reread the		
	problem.	reads and studies the problem carefully	problem if I don't understand it."		
		before proceeding.			
			Ask: "Now that I have read the problem, do I		
		'Ask' (Self-Question) Target: Does the	fully understand it?"		
		student fully understand the problem?			
			Check: "I understand the problem and will		
		'Check' (Self-Monitor) Target: Proceed only if	move forward."		
		the problem is understood.			
2.		'Say' (Self-Instruction) Target: The student	Say: "I will highlight key words and phrases		
	Paraphrase	restates the problem in order to demonstrate	that relate to the problem question."		
	the	understanding.			
	problem.		"I will restate the problem in my own words."		
		'Ask' (Self-Question) Target: Is the student			
		able to paraphrase the problem?	Ask: "Did I highlight the most important words		
			or phrases in the problem?"		
		'Check' (Self-Monitor) Target: Ensure that			
		any highlighted key words are relevant to the	Check: "I found the key words or phrases that		
		question.	will help to solve the problem."		
3.	'Draw' the	'Say' (Self-Instruction) Target: The student	Say: "I will draw a diagram of the problem."		
	problem.	creates a drawing of the problem to			
		consolidate understanding.	Ask: "Does my drawing represent the		
			problem?"		
		'Ask' (Self-Question) Target: Is there a match			

		between the drawing and the problem?	Check: "The drawing contains the essential parts of the problem."
		'Check' (Self-Monitor) Target: The drawing	parts of the problem.
		includes in visual form the key elements of the	
		math problem.	
4.	Create a	'Say' (Self-Instruction) Target: The student	Say: "I will make a plan to solve the problem."
	plan to	generates a plan to solve the problem.	
	solve the		Ask: "What is the first step of this plan? What
	problem.	'Ask' (Self-Question) Target: What plan will	is the next step of the plan?"
		help the student to solve this problem?	
			Check: "My plan has the right steps to solve
		'Check' (Self-Monitor) Target: The plan is	the problem."
		appropriate to solve the problem.	
5.	Predict/	'Say' (Self-Instruction) Target: The student	Say: "I will estimate what the answer will be."
	estimate	uses estimation or other strategies to predict	
	the Answer.	or estimate the answer.	Ask: "What numbers in the problem should be
		(2.11/2.16.2	used in my estimation?"
		'Ask' (Self-Question) Target: What	Charles "I did not alsia any increantant
		estimating technique will the student use to	Check: "I did not skip any important
		predict the answer?	information in my estimation."
		'Check' (Self-Monitor) Target: The	
		predicted/estimated answer used all of the	
		essential problem information.	
6.	Compute	'Say' (Self-Instruction) Target: The student	Say: "I will compute the answer to the
	the answer.	follows the plan to compute the solution to	problem."
		the problem.	
			Ask: "Does my answer sound right?" "Is my
		'Ask' (Self-Question) Target: Does the answer	answer close to my estimate?"
		agree with the estimate?	
			Check: "I carried out all of the operations in the
		'Check' (Self-Monitor) Target: The steps in	correct order to solve this problem."
		the plan were followed and the operations	
<u> </u>		completed in the correct order.	Co (1) The book has been a first and a fir
7.	Check the	'Say' (Self-Instruction) Target: The student	Say: "I will check the steps of my answer."
	answer.	reviews the computation steps to verify the	Ask: "Did I go through each step in my answer
		answer.	and check my work?"
		'Ask' (Self-Question) Target: Did the student	and effectiny work:
		check all the steps in solving the problem and	Check: ""
		are all computations correct?	
		and an acting attacked to a contract.	
		'Check' (Self-Monitor) Target: The problem	
		solution appears to have been done correctly.	
		solution appears to have been done correctly.	

Students will benefit from close teacher support when learning to combine the 7-step cognitive strategy to attack math word problems with the iterative 3-step metacognitive Say-Ask-Check sequence. Teachers can increase the likelihood that the student will successfully acquire these skills by using research-supported instructional practices (Burns, VanDerHeyden, & Boice, 2008), including:

- Verifying that the student has the necessary foundation skills to solve math word problems
- Using explicit instruction techniques to teach the cognitive and metacognitive strategies
- Ensuring that all instructional tasks allow the student to experience an adequate rate of success
- Providing regular opportunities for the student to be engaged in active accurate academic responding
- Offering frequent performance feedback to motivate the student and shape his or her learning.

References

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